Is dark matter with long-range interactions a solution to all small-scale problems of Λ CDM cosmology?

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The cold dark matter (DM) paradigm describes the large-scale structure of the universe remarkably well. However, there exists some tension with the observed abundances and internal density structures of both field dwarf galaxies and galactic satellites. Here, we demonstrate that a simple class of DM models may offer a viable solution to all of these problems simultaneously. Their key phenomenological properties are velocity-dependent self-interactions mediated by a light vector messenger and thermal production with much later kinetic decoupling than in the standard case.

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Introduction.— Recent advances of cosmological precision tests further consolidate the 'cosmological concordance model', indicating that 4.5% of the mass in the universe is in baryons, 22.6% is non-baryonic cold dark matter (CDM), and the rest is Einstein's cosmological constant Λ (or behaves like it) [1]. The leading CDM candidates are weakly interacting massive particles (WIMPs) which are thermally produced in the early universe [2]. While their *chemical* decoupling from the heat bath sets the observed DM relic density today, their kinetic decoupling induces a small-scale cutoff in the primordial power spectrum of density perturbations [3]. For neutralino DM, e.g., this cutoff corresponds to a smallest protohalo mass of $M_{\rm cut}/M_{\odot} \sim 10^{-11}$ – 10^{-3} [4], but it could be as large as $M_{\rm cut} \gtrsim 10\,M_{\odot}$ if DM couples to new light scalars [5]. After kinetic decoupling, standard WIMP CDM behaves like a collision-less gas. Baryons, on the other hand, can radiate away excess energy and sink to the centers of CDM halos where they form stars and galaxies. In this picture, structure formation proceeds hierarchically with galaxies to form at sites of constructive interference of small-scale waves in the primordial density fluctuations.

Despite the great success of Λ CDM cosmology, detailed observations of nearby small galaxies pose a number of puzzles to this paradigm. Here, we isolate three distinct classes of problems. (1) The observed galaxy luminosity and HI-mass functions show much shallower faint-end slopes than predicted by Λ CDM models [6]; this is locally known as the 'missing satellites problem' of the Milky Way (MW), which should contain many more dwarf-sized subhalos than observed [7]. (2) Simulations predict an inner DM cusp for the density structure of galaxies, seemingly at odds with the cored profiles found in observed low surface brightness galaxies and dwarf satellites [8]. (3) Recently, it was realized that the most massive subhalos in Λ CDM simulations of MW-size halos have an internal density structure that is too concentrated in comparison

to the observed brightest MW satellites: the simulated circular velocity profiles increase more steeply and attain their maximum circular velocity at smaller radii than any of the observed ones. On the other hand, those simulated subhalos should be 'too big to fail' in forming stars according to our understanding of galaxy formation (being more massive than the UV-photosuppression scale at all redshifts, after formation, for conceivable reionization histories). Thus, it is extremely puzzling why there is no observed analogue to those objects [9].

Astrophysical solutions to (1) invoke suppressing the formation of galaxies within existing dwarf halos or suppressing the star formation in dwarf galaxies. Galaxy formation can be held back by increasing the gas entropy before collapse, e.g. via photoionization [10], blazar heating [11] or AGN feedback in the radio-quiet mode [12]. A photoionization-induced lack of H_I [13] or intrinsically low metallicities [14] may further suppress the cooling efficiency of collapsing baryons. Numerical simulations with a photoionizing background, however, cannot suppress dwarf galaxy formation at the level implied by observations [15]. In principle, gas may also be removed from dwarfs via photo-evaporation [16] and feedback from supernovae [17]. Any such feedback, however, implies remnant stellar populations and HI masses in conflict with most recent observational constraints [18].

The 'cusp-core' problem (2) may be addressed by large velocity anisotropies or reduced central DM densities. There is a degeneracy between cored isotropic and cuspy anisotropic velocity distributions and the stellar line-of-sight velocity data is still too sparse to dynamically resolve (2) [19]. Reducing central DM densities was proposed as a result of efficient baryonic feedback processes [20], however in contradiction to cuspy dwarf profiles in other simulations with feedback [21].

The 'too big to fail' problem (3) might be solved by either an increased stochasticity of galaxy formation on

these scales or a total MW mass $\lesssim 8 \times 10^{11} \, \mathrm{M}_{\odot}$ [22]. Abundance matching of stellar and halo mass, which agree with stacking analyses of gravitational lensing signals and satellite dynamics of SDSS galaxies, make the required large degree of stochasticity implausible [23]. For a $10^{12} \, \mathrm{M}_{\odot}$ MW, on the other hand, the chance to host two satellites as massive as the Magellanic Clouds is less than 10% [24] and even lower for smaller MW masses (from satellites studies of MW-type SDSS systems [25] and MW and Andromeda orbit timing arguments [26]).

The next logical possibility that could lead to a suppression of small-scale power is a modification of the CDM paradigm itself. The most often discussed options are interacting DM (IDM) [27] and warm DM (WDM) [28], though it should be noted that there exist interesting alternatives such as DM from late decays [29], DM with large annihilation rates [30], extremely light DM particles forming a condensate [31], or inflationary models with broken-scale invariance [32]. As was soon realized, however, IDM with a constant cross section produces spherical cores in conflict with observed ellipticities in clusters [33] and the survivability of satellite halos [34]. While WDM is unlikely to account for some of the large $\sim 1 \, \rm kpc$ cores claimed in dwarfs [35], and severely constrained by Lyman- α observations [36–39], it may be able to partially resolve the 'too big too fail' problem by allowing these subhalos to initially form with lower concentrations [40]. Alternatively, DM self-interactions mediated by a Yukawa potential, with the resulting characteristic velocity dependence of the transfer cross section [41, 42], avoid constraints on scales of MW-type galaxies and beyond [43] and produce $\sim 1 \,\mathrm{kpc}$ cores that match the observed velocity profiles of massive MW satellites [44] (see also Ref. [41]).

Most astrophysical and DM solutions have shortcomings, or can explain at most two of the three problems, which makes them less attractive on the basis of Occam's razor. Here, we demonstrate that there is a class of IDM models that simultaneously can account for all three problems. Encouraged by the results of Refs. [43, 44], in particular, we will focus on models with a Yukawa-like interaction between the DM particles that is mediated by a light messenger (see Fig. 1). As we will show, the kinetic decoupling of DM in these models can happen sufficiently late to suppress the power spectrum at scales as large as that of dwarf galaxies, $M_{\rm cut} \gtrsim 10^9 M_{\odot}$, while at the same time the velocity-dependent self-interaction of DM produces cored density profiles in dwarfs ¹.

Model setup.— In models with new light exchange particles ϕ , kinetic decoupling can happen much later

than in standard WIMP scenarios, in particular for small masses m_{ϕ} [5]. For scalar exchange particles, however, the amplitude for DM scattering with leptons scales like $\sim m_{\chi} m_{\ell}/m_{\phi}^2$, implying that scattering with neutrinos is generally negligible. While a coupling of ϕ to charged leptons also leads to a loop-suppressed effective coupling to photons, $\mathcal{L} \supset g_{\phi\gamma\gamma}\phi F^{\mu\nu}F_{\mu\nu}$, the resulting scattering amplitude does not contribute in the relevant limit of small momentum transfer. Kinetic decoupling therefore never occurs at $T_{\rm kd} \ll 0.1\,{\rm MeV}$, at which point the number density of electrons starts to become strongly Boltzmann-suppressed and there are no lighter (and thus more abundant) particle species left that could keep up kinetic equilibrium instead.

Let us consider instead the situation where DM consists of heavy Dirac fermions χ which only couple to a light *vector* boson V. Due to our interest in late kinetic decoupling, we will require V to also couple to neutrinos:

$$\mathcal{L}_{\rm int} \supset -g_{\chi} \bar{\chi} V \chi - g_{\nu} \bar{\nu} V \nu \,. \tag{1}$$

Note that we take a phenomenological approach here and only state couplings that explicitly enter our analysis. In particular, V does not have to be a gauge boson, which leaves couplings to other SM particles unspecified (see e.g. Ref. [47] for a recent model-independent analysis). DM is then thermally produced in the early universe via $\bar{\chi}\chi \leftrightarrow VV$. Assuming g_{ν} is small, but large enough to thermalize V at early times, the relic density is given by

$$\Omega_{\chi} h^2 = \Omega_{\bar{\chi}} h^2 \simeq \frac{0.11}{2} \left(\frac{g_{\chi}}{0.683} \right)^{-4} \left(\frac{m_{\chi}}{\text{TeV}} \right)^2.$$
(2)

This expression receives $\mathcal{O}(1)$ corrections due to the Sommerfeld effect [48], i.e. a multiple exchange of V as shown in Fig. 1, which we fully take into account in our analysis. The kinetic decoupling temperature, on the other hand, will be set by χ - ν scattering. The corresponding amplitude at small momentum transfer reads

$$\sum_{\text{all spins}} |\mathcal{M}|_{\chi\nu\leftrightarrow\chi\nu}^2 = 64g_{\chi}^2 g_{\nu}^2 \frac{m_{\chi}^2 E_{\nu}^2}{m_V^4} \,. \tag{3}$$

In the following, we will consider g_{ν} as an essentially free parameter while g_{χ} is fixed by the requirement to obtain the correct relic density (see e.g. Ref. [49] for a list of possible natural explanations for $g_{\nu} \ll g_{\chi}$).

DM self-scattering.— The light vector messenger induces a long-range attractive Yukawa potential between the DM particles, cf. Fig. 1. Concerning elastic DM self-scattering, this is completely analogous to screened Coulomb scattering in a plasma for which simple parametrizations of the transfer cross section $\sigma_T(v)$ in terms of m_χ , m_V , g_χ and the relative velocity v of the DM particles exist [41, 50]. Using these parametrizations, it was shown that the type of DM model introduced above produces cores rather than cusps [43] and may solve the

 $^{^1}$ Late kinetic decoupling $(T_{\rm kd}\sim 0.1\,{\rm keV})$ was advocated as potential solution to the missing satellites problem before [45] – though this analysis considerably under-estimated $T_{\rm kd}$ for WIMPs [46].

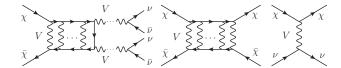


Figure 1: Interaction processes that set the DM relic density and may lead to observable neutrino annihilation products today (left), change the inner velocity and density profile of dwarf halos (middle) and induce a comparatively large cutoff in the spectrum of primordial density perturbations (right).

'too big too fail problem' [44], without being in conflict with the strong constraints for models with constant σ_T . We also note that σ_T drops with larger v such that for galaxy clusters only the very central density profile at $r \lesssim \mathcal{O}(1-10)$ kpc will be smoothed out, matching observational evidence (from improved lensing and stellar kinematic data [51]) for a density cusp in A383 that is slightly shallower than expected for standard CDM.

For our discussion, the astrophysically important quantities are the velocity $v_{\rm max}^2 = g_\chi^2 m_V/(2\pi^2 m_\chi)$ at which $\sigma_T v$ becomes maximal and $\sigma_T^{\rm max} \equiv \sigma_T (v_{\rm max}) = 22.7 \, m_V^{-2}$. In particular, $v_{\rm max}$ should not be too different from the typical velocity dispersion $\sigma_v \sim \mathcal{O}(10)\,\mathrm{km/s}$ encountered in dwarf galaxies if one wants to make any contact to potential problems with standard structure formation at these scales. On the other hand, the value of $\sigma_T^{\rm max}$ is constrained by various astrophysical measurements, see Ref. [44] for a compilation of current bounds.

Fixing g_{χ} by the relic density requirement, there is a one-to-one correspondence between the particle physics input (m_{χ}, m_V) and the astrophysically relevant parameters $(v_{\rm max}, \sigma_T^{\rm max})$. As demonstrated in Fig. 2, a solution to the aforementioned small-scale problems (2) and (3) may then indeed be possible for DM masses of $m_{\chi} \gtrsim 600\,{\rm GeV}$ and a mediator mass in the (sub-) MeV range. We also display the strongest astrophysical bounds on large DM self-interaction rates [43]. For $m_{\chi} \lesssim 4\,{\rm TeV}$, they arise from collisions with particles from the dwarf parent halo, while at larger m_{χ} an imminent gravothermal catastrophe is more constraining.

The small-scale cutoff.— For small kinetic decoupling temperatures $T_{\rm kd}$, acoustic oscillations [52] are more efficient than free streaming effects to suppress the power spectrum [4, 53]. The resulting exponential cutoff can be translated into a smallest protohalo mass of

$$M_{\rm cut} \approx \frac{4\pi}{3} \left. \frac{\rho_{\chi}}{H^3} \right|_{T=T_{\rm kd}} = 1.7 \times 10^8 \left(\frac{T_{\rm kd}}{\rm keV} \right)^{-3} M_{\odot} \,, \quad (4)$$

where H is the Hubble rate and we assumed late kinetic decoupling such that the effective number of relativistic degrees of freedom $g_{\text{eff}} = 3.37$. For scattering with relativistic neutrinos, c.f. Eq. (3), the analytic treatment of kinetic decoupling given in Ref. [54] is valid. Extending

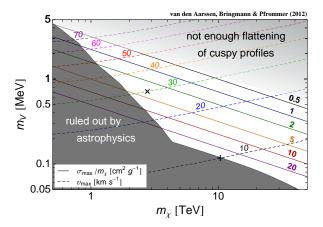


Figure 2: The white area corresponds to DM and mediator masses that may solve the 'cusp vs. core' problem. The crosses indicate two benchmark models for which detailed simulations [44] have found a solution to the 'too big to fail' problem. Dashed and solid lines show contours of the astrophysical relevant quantities $\sigma_{\rm max}^{\rm T}$ and $v_{\rm max}$. See text for further details.

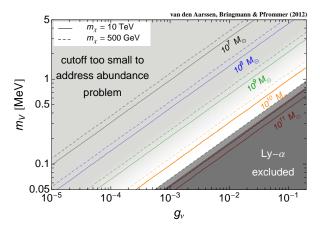


Figure 3: This plane shows the mediator mass m_V vs. the coupling strength g_{ν} . Large values of g_{ν} and small values of m_V lead to late kinetic decoupling and thus a large mass $M_{\rm cut}$ of the smallest protohalos. $M_{\rm cut} \gtrsim 5 \times 10^{10} M_{\odot}$ is excluded by Ly- α data while $M_{\rm cut} \gtrsim 10^9 M_{\odot}$ may solve the small-scale abundance problems of $\Lambda{\rm CDM}$ cosmology.

those expressions to allow for $T_{\nu} \neq T$, we find

$$T_{\rm kd} = \frac{0.062 \,\text{keV}}{N_{\nu}^{\frac{1}{4}} \left(g_{\chi}g_{\nu}\right)^{\frac{1}{2}}} \left(\frac{T}{T_{\nu}}\right)_{\rm kd}^{\frac{1}{2}} \left(\frac{m_{\chi}}{\text{TeV}}\right)^{\frac{1}{4}} \left(\frac{m_{V}}{\text{MeV}}\right) , \quad (5)$$

where N_{ν} is the number of neutrino species coupling to V. Combining this with Eq. (2) we therefore expect that $T_{\rm kd}$, and thus $M_{\rm cut}$, is essentially independent of g_{χ} and m_{χ} .

Using for definiteness $N_{\nu}=3$ and $T_{\nu}=(4/11)^{\frac{1}{3}}T_{\gamma}$, we show in Fig. 3 contours of constant $M_{\rm cut}$ in the (g_{ν},m_V) plane. We find that the result of the full numerical calculation [4, 5] is indeed extremely well described by Eqs. (4,5) for $g_{\nu}\gtrsim 10^{-7}$ (assuming $m_{\chi}\sim 1\,{\rm TeV}$ and $m_V\sim 1\,{\rm MeV}$; this value is even lower for larger m_{χ} and

smaller m_V). For $g_{\nu} \lesssim 10^{-7}$, DM scattering with the non-relativistic mediator particles V starts to dominate over scattering with neutrinos, and $M_{\rm cut}$ eventually becomes independent of g_{ν} . We checked that the new era of DM annihilation generally expected in models with Sommerfeld-enhanced annihilation rates (see Ref. [5] for a consistent treatment) has only negligible impact on our results for the late decoupling times we focus on here.

Lyman- α forest bounds.— Conventionally, a possible cutoff in the power spectrum is often expressed in terms of the mass $m_{\rm w}$ of a WDM thermal relic. In this case, it is set by free streaming of the WDM particles and the comoving free-streaming length $R_{\rm f}$ is given by $R_{\rm f} = 0.1 \left(\Omega_{\rm m} h^2/0.13\right)^{1/3} \left(m_{\rm w}/{\rm keV}\right)^{-4/3} {\rm Mpc}$ [55]. For a characteristic wavenumber $k_{\rm f} \equiv 0.46/R_{\rm f}$, the linear perturbation amplitude is suppressed by a factor of 2 and the characteristic filtering mass can be defined as [55]

$$M_{\rm f} \equiv \frac{4\pi}{3} \,\bar{\rho}_{\rm m} \, \left(\frac{\lambda_{\rm f}}{2}\right)^3 = 5.1 \times 10^{10} \left(\frac{m_{\rm w}}{\rm keV}\right)^{-4} {\rm M}_{\odot} \,, \quad (6)$$

where $\lambda_{\rm f}=2\pi/k_{\rm f}\simeq 13.6R_{\rm f}$. This choice of $M_{\rm f}$ is justified by numerical experiments [56] that find the resulting halo statistics for an initial density distribution with a sharp cut in the power spectrum at $k_{\rm c}=2\pi/\lambda_{\rm f}$ to be very similar to the statistics of an initial density field smoothed with a top-hat window of radius $\lambda_{\rm f}/2$. Cosmological WDM simulations show a deviation of the mass function from the CDM case on scales given by Eq. (6) [6, 57].

Combining data of the Lyman- α forest, the cosmic microwave background (CMB) and galaxy clustering allows to constrain the cutoff scale in the power spectrum; in terms of the mass of a thermal WDM candidate, a 2σ -bound of $m_{\rm w} > 2\,{\rm keV}$ has been claimed [36, 37]. This weakens to $m_{\rm w} > 0.9\,{\rm keV}$ when rejecting less reliable data at z > 3.2 [36] due to systematic errors [38]. Revisiting Lyman- α data yielded $m_{\rm w} > 1.7\,{\rm keV}$ which, however, is subject to systematic uncertainties at the $\sim 30\%$ level [39], especially considering that blazar heating was not accounted for in deriving cosmological constraints [58].

Lyman- α data thus firmly exclude $m_{\rm w} < 1\,{\rm keV}$ or $M_{\rm f} > 5.1 \times 10^{10}\,{\rm M}_{\odot}$ (corresponding to a maximal circular velocity $v_{\rm max} \sim 70\,{\rm km~s}^{-1}$). For $m_{\rm w} \simeq 1-2\,{\rm keV}$, WDM models are able to alleviate the 'missing satellite problem' (somewhat depending on feedback recipes) [59], bring the faint-end of the galaxy luminosity function into agreement with data [60], and match [6] the HI velocity function measured in the ALFALFA survey ². For $m_{\rm w} > 3\,{\rm keV}$, the corresponding mass cutoff $M_{\rm f} < 6 \times 10^8\,{\rm M}_{\odot}$ is too small to have any impact on the

faint-end of the galaxy luminosity function. We include these bounds in Fig. 3 to demonstrate that our model can successfully address also the abundance problem (1).

Discussion.— In a phenomenological approach to identify the key properties of DM models that can address all three Λ CDM small-scale problems simultaneously, we found it sufficient to simply postulate the existence of a light vector messenger V that couples to both DM and neutrinos as in Eq. (1). If V does not couple to quarks or other leptons, the coupling g_{ν} is essentially unconstrained [47]. While beyond the scope of this letter, however, we stress that it would be very worthwhile to study possible concrete realizations of our setup.

The greatest challenge for such a model building might be to prevent, even at the one-loop level, a kinetic mixing between V and photons, which is severely constrained for $m_V \lesssim \text{MeV}$ [62]. On the other hand, limits on tree-level couplings of V to charged leptons (e.g. from contributions to the anomalous magnetic moment of the muon, beam dump experiments or low- $|q|^2 \nu$ -e scattering [62, 63]) seem less severe and could at least partially be evaded by generation-specific couplings. Another option could be a new U(1) coupling to DM and sterile neutrinos ν_s [64]. As long as the ν_s have been in equilibrium in the very early universe and are relativistic at $T_{\rm kd}$, this would not change the phenomenology of our model; Eq. (5), in particular, would still apply. It is therefore quite interesting that CMB observations seem to favor additional relativistic degrees of freedom, which corresponds to the presence of one light sterile neutrino species [65].

Finally, we note that for typical galactic velocities $v \sim 10^{-3}$, the type of DM candidate we propose here annihilates with a Sommerfeld-enhanced rate of $\langle \sigma v \rangle \sim 3 \times 10^{-24} \ (m_\chi/{\rm TeV})^{-2} {\rm cm}^3 {\rm s}^{-1}$ into a VV pair which then decays exclusively into neutrinos (if $m_V \leq 2m_e$). Such a large annihilation rate will be in reach of future IceCube observations of the galactic center [66]; for $m_\chi \lesssim 1 \,{\rm TeV}$, in fact, a strong Sommerfeld-induced substructure enhancement of the signal [67] may already be constrained.

Conclusions.— We have introduced a class of DM models with the unique property of addressing all three Λ CDM small-scale problems simultaneously, which should make them very attractive alternatives to be studied. From a model-building point of view, the only ingredient that is needed is a (sub-)MeV vector messenger particle that weakly couples to neutrinos and even more weakly to other standard model particles. While collider and direct searches for DM will be extremely challenging in this scenario, a TeV neutrino signal from the galactic center could turn out to be a smoking gun signature.

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² The small-end of simulated velocity functions for a thermal relic WDM particle with $m_{\rm w}\lesssim 3$ keV are noticeably shallower than the analytical estimates of the Sheth and Tormen [61].

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